

**KAKATIYA UNIVERSITY**  
**M.A. /M.Sc. MATHEMATICS Syllabus (w.e.f.2019-20)**  
**Semester –IV**  
**Paper – I**  
**Paper Code: M4CP1**  
**ADVANCED LINEAR ALGEBRA**

Review of Vector Spaces-Subspaces- Bases and Dimension-Coordinates.

**UNIT I**

Linear Transformations-The algebra of Linear Transformations – Isomorphism - Representation of Transformations by Matrices - Linear Functionals.  
(Chapter 3: Sec 3.1 to 3.5 of the Text Book)

**UNIT II**

The double Dual - Characteristic Values - Annihilating Polynomials - Cayley Hamilton Theorem-Invariant Subspaces.  
(Chapter 3: Sec 3.6, Chapter 6: Sec 6.1 to 6.4 of the Text Book)

**UNIT III**

Direct-sum Decompositions - Invariant Direct sums - The primary Decomposition theorem-Cyclic Subspaces and Annihilators – Statement of Cyclic Decompositions Theorem and its applications (except Generalized Cayley -Hamilton Theorem)- Rational Form.  
(Chapter 6: Sec 6.6 to 6.8, Chapter 7: Sec 7.1 to 7.2 of the Text Book)

**UNIT IV**

Bilinear Forms: Bilinear forms - Symmetric Bilinear Forms - Skew Symmetric Bilinear Forms - Groups preserving Bilinear Forms  
(Chapter 10: Sec 10.1 to 10.4 of the Text Book)

**Text Book:**

Linear Algebra by Kenneth Hoffman and Ray Kunze, 2<sup>nd</sup> Edition, Pearson (2003).

**Reference Books:**

1. Finite Dimensional Vector Spaces by p.Halmos,D Vanostrand,Princeton.
2. Linear Algebra by H.Friedberg etal, PHI(2007)
3. Linear Algebra by Lipschitz, Schaum Series.

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**M.A. /M.Sc. MATHEMATICS Syllabus (w.e.f.2019-20)**  
**Semester –IV**  
**Paper – II**  
**Paper Code: M4CP2**  
**GRAPH THEORY**

**UNIT – I**

Relations and Digraphs

Relations and Digraphs – Special Properties of Binary Relations – Equivalence Relations – Ordering Relations – Lattices and Enumerations – Paths and Closures – Directed Graphs and Adjacency Matrices

**UNIT – II**

Graphs

Basic Concepts – Isomorphism and Subgraphs – Trees and their properties – Spanning Trees – Directed Trees – Binary Trees – Planar Graphs.

**UNIT – III**

Multigraphs

Euler’s Formula – Konigsberg Seven Bridges problems – Multigraphs – Euler Circuits – Hamiltonian Graphs – Chromatic Numbers – The Four–Colour Problem.

**UNIT – IV**

Net works flows

Graphs as Models of Flow of Commodities – Flows – Maximal Flows and Minimal cuts- The Maxflow Min- Cut Theorem – Applications – Matching and Hall’s Marriage Theorem.

**TEXT BOOK :**

Discrete Mathematics for Computer Scientists and Mathematicians By J.L. Mott.  
A. Kandle, P.Bakes.

**REFERENCE BOOKS:**

1. A First Book at Graph Theory – By John Clark and Derek Allan Hotton.
2. Discrete Mathematical Structures & Graph Theory – By Rao
3. A Text Book of Graph Theory and its applications – By B. Suryanarayana and G.K. Ranganath.

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**Semester –IV**  
**Paper – III**  
**Paper Code: M4CP3**  
**INTEGRAL EQUATIONS AND TRANSFORMS**

**UNIT I**

Integral Equation – Differentiation of a Function under an Integral Sign – Relation Between Differential and integral Equations – Solution of Non-homogeneous Volterra’s Integral Equations by the method of Successive Substitution and Successive Approximation of some Resolvent Kernels – Volterra Integral Equation of First Kind.  
 (Sec 1.1 to 2.4 of Text Book 1)

**UNIT II**

Solution of the Fredholm Integral Equation by the Method of Successive Substitution and successive approximation – Reciprocal Functions - Volterra’s Solution of Fredholm’s Equation – Statement of Fredholm first Theorem- Statement of Unique Solution of the Non-homogeneous Fredholm Integral Equation – Integral equations with degenerate kernels - Symmetric Kernel – Eigen value of a Symmetric kernel- Real Characteristic Constants.  
 (Sec 2.5 to 2.9, 3.1, 3.2, 3.14 and 4.1, 4.4, 4.5. of Text Book 1)

**UNIT III**

Laplace Transforms – Existence of Laplace Transform – Properties of Laplace Transform- The inverse Laplace transform and properties – Convolution Theorem- Solution of ordinary differential Equations by Laplace Transforms- Solution of Ordinary Differential Equations with variable coefficients by Laplace Transforms.-  
 (Chapter 1, Chapter 2: Sec 2.1 to 2.15, Chapter 3: Sec 3.1, 3.2, of Text Book 2)

**UNIT IV**

Fourier Transforms – Fourier Integral Formula – Inversion Theorem for Complex Fourier Transform -Fourier Sine and Cosine Transform - Inversion of Formulae – Convolution Theorem- Parseval’s identity -Finite Fourier Sine and Cosine Transforms - Inversion Formulae -Operational Properties – Convolution.  
 (Chapter 6: Sec 6.1 to 6.15, 6.17, 6.18, 6.19, Chapter 7: Sec 7.1 to 7.4, 7.6, 7.7, 7.9, of Text Book 2)

**Text Book:**

1. Integral Equations by Shanty Swarup
2. Integral Transforms by A. R Vasistha and R.K. Gupta

**Reference Book:**

Advance Calculus for Applications by Francis B. Hilder Brand Prentic Hall of India

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**M.A. /M.Sc. MATHEMATICS Syllabus (w.e.f.2019-20)**  
**Semester –IV**  
**Paper – IV (Elective)**  
**Paper Code: M4OP4(1)**  
**NEAR RINGS**

**UNIT I**

The Structure Of Near –Rings: Near-ring - The Near-Ring of all mappings on a group  $G$  - The Near-Ring of all zero respective mappings on  $G$  - Sub-Near-Ring - Abelian Near-Ring - Commutative Near-Ring - Zero Near-Ring - Zero Symmetric Near-Ring - Constant Near-Ring - Trivial Zero Symmetric Near-Ring and Trivial Constant Near-Ring - Near-ring homomorphism and isomorphism - Ideal (left, right ) of a Near-Ring - Quotient Near-Ring - Natural homomorphism associated with an Ideal - Kernel of homomorphism - R-sub group (left, right) of a Near-Ring  $R$  - Simple Near-Ring.  
(Chapter 1: Sec 1.1 to 1.40 of the Text Book)

**UNIT II**

Near-Ring Modules: R-module - Faithful representation - Centralizer Near-Ring - The right regular representation of a Near-Ring - R-sub module - Unital R-module - R-module homomorphism and isomorphism - Quotient R-module - Annihilator of a subset.  
(Chapter 2: Sec 2.1 to 2.37 of the Text Book)

**UNIT III**

Primitive Near-Rings: Homogenic Near-Ring - R-module of type 0 - R-module of type 1 - R-module of type 2 - V-primitive Near-Ring - The Stabilizer.  
(Chapter 3: Sec 3.1 to 3.37 of the Text Book)

**UNIT IV**

More on 2-Primitive Near-Rings: Rank – Projection - Minimal condition - Maximal condition – DCCS – DCCR – DCCI – ACCR – ACCI  
(Chapter 4: Sec 4.1 to 4.28 of the Text Book)

**Text Book:**

Near-Rings and their links with groups by J.D.P.Meldrum.

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**Semester –IV**  
**Paper – IV (Elective)**  
**Paper Code: M4OP4 (2)**

**THEORY OF ORDINARY DIFFERENTIAL EQUATIONS**

**UNIT I**

System of Linear Differential Equations: Introduction system of First order Equations - Existence and Uniqueness theorem - Fundamental Matrix - Non Homogenous Linear System - Systems with Constant Coefficients – Linear Systems with Periodic Co-efficient (Chapter 4: Sec 4.1 to 4.7 of Text Book)

**UNIT II**

Existence and Uniqueness of Solutions : Introduction – Preliminaries - Successive Approximations - Picard’s Theorem - Non Uniqueness of Solutions - Continuation and Dependence on initial conditions - Existence of Solutions in the large - Existence and Uniqueness of Solutions of Systems. (Chapter 5: Sec. 5.1. to 5.8 of Text Book)

**UNIT III**

Behavior of Solutions of linear Differential Equations : Introduction -  $n^{\text{th}}$  order - Elementary Critical Points - Critical Points of Non-Linear system - Linear Systems with Constant-coefficient - Linear Systems with variable Co-efficient - Second Order Linear Differential Equations . (Chapter 5 & 6 of Text Book)

**UNIT IV**

Stability Non-Linear systems : Introduction - Stability of Quasi- Linear Systems - Stability of Autonomous Systems - Stability of Non- Autonomous Systems - A special Lyapanov Function (Chapter 9: Sec 9.1 to 9.5 of Text Book)

**Text Book:**

Ordinary Diff. Equations and Stability Theory by S.G. Deo, V. Ragvendra and V.Laxmi Kantham.

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**Semester –IV**  
**Paper – IV(Elective)**  
**Paper Code: M4OP4(3)**  
**OPERATIONS RESEARCH**

**UNIT I:**

Sequencing and Scheduling: Sequencing Problem – The Problem of n Jobs and Two Machines – Problem with n Jobs and m Machines – General Problem of n Jobs and m Machines - Scheduling – Critical Path Determination by CPM – Critical Path Determination by PERT – Optimum Scheduling by CPM.

(Chapter 7 of Text Book1)

**UNIT II**

Queueing Theory – Introduction – Queueing system – Elements of a Queueing system – Operating characteristics of a Queueing system – Deterministic Queueing system – Probability distributions in Queueing systems – Classification of Queueing Models – Definition of Transient and Steady States – Poisson Queueing systems.

(Chapter 21: Sec 21.1 to 21.9 of Text Book 2)

**UNIT III**

Dynamic Programming – Introduction – The recursive equation approach – Characteristics of Dynamic Programming – Dynamic Programming Algorithm – Solution of L.P.P. by Dynamic Programming.

(Chapter13: Sec 13.1 to 13.4, 13.7 of Text Book 2)

**UNIT- IV**

Non-Linear Programming – General Non – Linear Programming Problem – Constrained Optimization with Equality Constraints - Constrained Optimization with Inequality Constraints – Non – Linear Programming Methods – Graphical Solution – Quadratic Programming – Wolfe’s Modified Simplex Method – Beale’s Method.

(Chapter 27: Sec 27.3 to 27.5, Chapter 28:Sec 28.1, 28.2, 28.4 to 28.6 of Text Book 2)

**Text Book:**

1. Introduction to Optimization Operations Research by J.C. Pant(6<sup>th</sup> Edition)
2. Operations Research by Kanthi Swarup, P.K.Gupta, Man Mohan, Sultan Chand & Sons

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**Semester –IV**  
**Paper –IV (Elective)**  
**Paper Code: M4OP4 (4)**

**Computational Methods for Partial Differential Equations**

**UNIT I**

Partial Differential Equations – Introduction – Difference Method – Routh Hurwitz Criterion – Domain of Dependence of Hyperbolic Equations.  
(Chapter 1: Sec 1.1 to 1.4 of Text Book)

**UNIT II**

Difference Methods for Parabolic Differential Equations – Introduction – One Space Dimension – Two Space Dimensions – Spherical and Cylindrical Coordinate System.  
(Chapter 2: Sec 2.1 to 2.3, 2.5 of Text Book)

**UNIT III**

Difference Methods for Hyperbolic Partial Differential Equations – One Space Dimensions – Two Space Dimensions – First Order Equations.  
(Chapter 3: Sec 3.1 to 3.4 of Text Book)

**UNIT- IV**

Numerical Methods for Elliptic Partial Differential Equations – Introduction – Difference Methods for Linear Boundary Value Problems – General Second Order Linear Equation – Equation in Polar Coordinates.  
(Chapter 4: Sec 4.1 to 4.4 of Text Book)

**Text Book :**

Computational Methods for Partial Differential Equations by M.K.Jain, S.R.K.Iyengar, R.K.Jain, Wiley Eastern Limited, New Age International Limited, New Delhi

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**Semester –IV**  
**Paper –IV (Elective)**  
**Paper Code: M4OP4 (5)**  
**AUTOMATA AND MACHINES**

**UNIT I**

Context - Free Languages : Context – Free languages – Derivation Trees- Ambiguity in Context – Free Grammars – Simplification of Context – Free Grammars – Combsky Normal Form of Context - Free Grammars – Pumping Lemma for context – Free Languages- Decision Algorithms for Context – Free Languages.

**UNIT II**

Pushdown Automata : Basic Definitions – Acceptance by Pda – Pushdown Automata and Context Free Languages- Parsing and Push Down Automata.

**UNIT III**

Turning Machines And Linear Bounded Automata: Turning Machine Model – Representation of Turning Machines – Language Acceptability by Turing Machines – Design of Turing Machines – Universal Turing Machines and their Modifications. The Model of Linear Bounded Automata – Turing Machines and Type O Grammars.

**UNIT IV**

Linear Bounded Automata and languages – Halting Problem of Turing Machines – NP – Completeness – LR (K) Grammars – Properties of LR(K) Grammars – Closure Properties of Languages.

**Text Book:**

Theory of Computer Science (Automata, languages and Computation) by KLP Mishra and N.Chandrasekhar, Printice Hall of India.



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**Semester –IV**  
**Paper –IV (Elective)**  
**Paper Code: M4OP4 (6)**  
**THEORY OF RELIABILITY**

**UNIT I**

Reliability – Definition of Reliability - Failure Data Analysis – Failure data – Mean failure rate – Mean time to failure – Mean time between failures – Graphical plots – MTTF in terms of failure density – Generalization - Reliability in terms of Hazard rate and failure density – Mean time to failure in integral form - Hazard Models: Constant Hazard, Linearly increasing Hazard – The Weibull model – Distribution functions and reliability analysis – Some important distributions - Expected value — Standard deviation and variation.  
(Chapter 2, Chapter 3: Sec 3.1 to 3.11, Chapter 4: Sec 4.1 to 4.4, 4.6, 4.7, 4.9, 4.10 of Text Book1)

**UNIT II**

Interference Theory and Reliability Computations – General expression for reliability – Reliability computation for normally distributed stress and strength – Reliability computation for Log normally distributed stress and strength – Reliability computation for exponentially distributed stress and strength - Reliability computation for normally(exponentially) distributed strength and exponentially(normally) distributed stress - Reliability computation for gamma distributed stress and strength- Reliability computation for weibull distributed stress and strength.  
(Chapter 6: Sec 6.1, 6.2, 6.3, 6.4, 6.5, 6.6, 6.8 of Text Book 2)

**UNIT III**

System Reliability – Series configuration – Parallel configuration – Mixed configuration – Application to specific hazard models – An r-out of –n structure – Methods of solving complex systems – Systems not reducible to mixed configuration - Mean time to failure of systems - Logic diagrams – Markov models – Markov graphs.  
(Chapter 6: Sec 6.1 to 6.12 of Text Book 1)

**UNIT IV**

Reliability improvement – Improvement of components – Redundancy - Element Redundancy - Unit Redundancy - Standby Redundancy.  
Maintainability and availability - Maintainability – Availability.  
Repairable systems – Instantaneous repair rate – Mean time to repair – Reliability and availability functions.  
(Chapter 7: Sec 7.1 to 7.6, Chapter 9: Sec 9.1 to 9.3, chapter 10 of Text Book 1)

**Text Books:**

1. Reliability Engineering by L.S. Srinath, Fourth edition, East-West Press Private Limited.
2. Reliability in Engineering Design by K.C.Kapur, L.R.Lamberson, John Wiley & Sons, Inc.

**Reference Books:**

Reliability Engineering by E.Balagurusamy, Tata McGraw-Hill Publishing Company Limited.

**M4OP5(1)**

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**Semester –IV**  
**Paper – V (Elective)**  
**Paper Code: M4OP5 (1)**  
**PROGRAMMING METHODOLOGY**

**UNIT I**

Algorithms – Data-Data types and primitive operations – Variables and Expressions - From Algorithms to Programs Decisions Structures – Looping – Use of Compound conditions – Case Statement Applications

**UNIT II**

Sub Algorithms – Argument – Parameter Correspondence – Recursive Sub algorithms – Applications composite Date Structures One- Dimensional Arrays – Sorting and Searching with Vectors – Application of Vectors.

**UNIT III**

Higher – Dimensional Arrays – Application of Arrays – Files – Linear Data Structures – Linear Lists- Storage Structure Concepts – Sequential Storage Structure for Arrays – Application of Stacks – Queues.

**UNIT IV**

Non-Linear Data Structures – Trees – General Trees – Application of Trees- Graphs.

**Text Book :**

Introduction to Computer Science by Trembay and Bunt.

**Lab Work :**

Simple programs in C on the above Structures

**Pattern of Lab Training.**

The total number of students are made into batches. The number of students in each batch should not more than students and each batch should be handled by two teachers

**M4OP5(2)**

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**Semester –IV**  
**Paper – V (Elective)**  
**Paper Code: M4OP5 (2)**  
**PROGRAMMING IN C++**

**UNIT I**

Input and Output in C++-C++ Declarative control Structures .  
(Chapters 2, 3 and 4 of Text Book)

**UNIT II**

Functions in C++ - Classes and Objects.  
(Chapters 5 and 6 of Text Book)

**UNIT III**

Constructors and Destructors – Operator Overloading and Type conversion – Inheritance  
(Chapters 7, 8 and 9 of Text Book)

**UNIT IV**

Pointers and Array – C++ and Memory – Binding , Polymorphism and Virtual Functions  
(Chapters 10, 11 and 12 of Text Book)

**Text Book:**

Object-Oriented Programming with ANSI & Turbo C++ by Ahok. N. Kamthane.

**Lab Work:**

Simple programs in C ++ on the above topics.

**Pattern of Lab Training :**

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**M4OP5 (3)**

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**Semester –IV**  
**Paper – V (Elective)**  
**Paper Code: M4OP5 (3)**  
**APPLIED STOCHASTIC PROCESS WITH MAT LAB**

**UNIT I**

Stochastic Process: Some Notations – Introduction - Specifications of Stochastic Process - Stationary process.

(Sec 2.1, 2.2 & 2.3 of Text Book 1)

Markov chains: Definition and Examples - Transition Matrix - Order of Markov chains - Markov chain as graphs - Higher transition probabilities - Classification of States and chains – Irreducible chain - periodic chain - transient and recurrence states - first passage time distributions - stability of Markov system - Stationary distribution - Ergodicity.

(Sec 3.1, 3.2, 3.4, 3.6 of Text Book 1)

**UNIT II**

Markov Process with Discrete State Space - Poisson process - Poisson process and related distributions - Continuous Time Markov Chain (CTMC).

(Sec 4.1, 4.2 & 4.5 of Text Book 1)

**UNIT III**

Finite Markov Chains and its Applications: Finite Markov chains with recurrent & transient States - Irreducible finite Markov Chains with Ergodic states, statistical inference.

(Sec 5.1, 5.2 & 5.3 of Text Book 2 )

**UNIT IV**

Stationary Process and Time Series : Introduction - Models of time series - Time and frequency domain - Power spectrum Statistical Analysis of Time Series - Some definitions

(Sec 8.1, 8.2, 8.3 & 8.4 of Text Book 1 )

**Text Book:**

1. Stochastic Process by J.Medhi, Second Edition, Wiley Eastern Limited
2. Elements of Applied Stochastic Process by U.N.Bhatt, JohnWiley & Sons

**Reference Books:**

1. Stochastic Process by N.U. Prabhu, Macmillan, NewYork

**PRACTICALS**

**(20 Marks)**

**i) Lab Work (MATLAB)**

**(10 Marks)**

1. Basic Matrix operations
2. Computation of Eigen values & Eigen vectors.
3. Computation of steady state probability distribution using
  - a. Power method
  - b. Jacobi method
  - c. Gauss-Seidel method

**Reference Books:**

1. Getting Started with MATLAB by Rudra Pratap, Oxford University Press.
2. Introduction to Numerical Solutions of Markov Chains by William J. Stewart, Princeton University Press.

**ii. Case Studies**

**(10 Marks)**

Applications of finite Markov Chains in Finance and Banking, Health Care, Retail Business, Internet Traffic Modeling and other research and development areas.

Note: For the case studies, students will be divided into batches. Each batch consists of two or three students.

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**Paper Code: M4OP4 (6)**  
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(Chapter 2, Chapter 3: Sec 3.1 to 3.11, Chapter 4: Sec 4.1 to 4.4, 4.6, 4.7, 4.9, 4.10 of Text Book1)

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(Chapter 6: Sec 6.1, 6.2, 6.3, 6.4, 6.5, 6.6, 6.8 of Text Book 2)

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(Chapter 6: Sec 6.1 to 6.12 of Text Book 1)

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Repairable systems – Instantaneous repair rate – Mean time to repair – Reliability and availability functions.  
(Chapter 7: Sec 7.1 to 7.6, Chapter 9: Sec 9.1 to 9.3, chapter 10 of Text Book 1)

**Text Books:**

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2. Reliability in Engineering Design by K.C.Kapur, L.R.Lamberson, John Wiley & Sons, Inc.

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